

Mark Scheme (Results)

October 2022

Pearson Edexcel International Advanced Level In Statistics S1 (WST01) Paper 01

Edexcel and BTEC Qualifications

Edexcel and BTEC qualifications are awarded by Pearson, the UK's largest awarding body. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information visit our qualifications websites at <u>www.edexcel.com</u> or <u>www.btec.co.uk</u>. Alternatively, you can get in touch with us using the details on our contact us page at <u>www.edexcel.com/contactus</u>.

Pearson: helping people progress, everywhere

Pearson aspires to be the world's leading learning company. Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: www.pearson.com/uk

October 2022 Question Paper Log Number P72154A Publications Code WST01_01_2210_MS All the material in this publication is copyright © Pearson Education Ltd 2022

General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.

2. The Edexcel Mathematics mark schemes use the following types of marks:

<u>'M' marks</u>

These are marks given for a correct method or an attempt at a correct method. In Mechanics they are usually awarded for the application of some mechanical principle to produce an equation. e.g. resolving in a particular direction, taking moments about a point, applying a suvat equation, applying the conservation of momentum principle etc.

The following criteria are usually applied to the equation.

To earn the M mark, the equation

(i) should have the correct number of terms

(ii) be dimensionally correct i.e. all the terms need to be dimensionally correct

e.g. in a moments equation, every term must be a 'force x distance' term or 'mass x distance', if we allow them to cancel 'g' s.

For a resolution, all terms that need to be resolved (multiplied by sin or cos) must be resolved to earn the M mark.

M marks are sometimes dependent (DM) on previous M marks having been earned. e.g. when two simultaneous equations have been set up by, for example, resolving in two directions and there is then an M mark for solving the equations to find a particular quantity – this M mark is often dependent on the two previous M marks having been earned.

<u>'A' marks</u>

These are dependent accuracy (or sometimes answer) marks and can only be awarded if the previous M mark has been earned. E.g. M0 A1 is impossible.

<u>'B' marks</u>

These are independent accuracy marks where there is no method (e.g. often given for a comment or for a graph)

A few of the A and B marks may be f.t. – follow through – marks.

3. General Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- ***** The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:

If all but one attempt is crossed out, mark the attempt which is NOT crossed out. If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

Special notes for marking Statistics exams (for AAs only)

- Any correct method should gain credit. If you cannot see how to apply the mark scheme but believe the method to be correct then please send to review.
- For method marks, we generally allow or condone a slip or transcription error if these are seen in an expression. We do not, however, condone or allow these errors in accuracy marks.

Question Number	Scheme	Marks					
1. (a)	$[\text{Area} = k \times \text{frequency} \rightarrow 16.5 = k \times 12 \rightarrow] \text{Area} = \frac{16.5}{12} \times 18 \text{ oe}$ $= \underline{24.75} \text{ (cm}^2)$	M1 A1 (2)					
(b)	fd method $\frac{24}{58-55}[=8]$ and $\frac{35}{55-50}[=7]$ or Area method $\frac{16.5}{12} \times 24[=33]$ and $\frac{16.5}{12} \times 35[=48.125]$ or $\frac{16.5}{12} \times \frac{24}{3}[=11]$ and $\frac{16.5}{12} \times \frac{35}{5}[=9.625]$ Let h = height of the 2 nd tallest bar	M1					
	$[h=]\frac{10}{8} \times 7'$ or $[h=]\frac{48.125 \times 10 \times 3}{5 \times 33}$ or $[h=]^{9.625} \times \frac{10}{11}$ = <u>8.75 (cm</u>)	dM1 A1 (3)					
	$[Q_2 =]50 + \frac{7}{35} \times 5$ or $[Q_2 =]55 - \frac{28}{35} \times 5$ = <u>51</u> (cm)	M1 A1					
(ii)	$[Q_3 =]55 + \frac{2}{24} \times 3$ or $[Q_3 =]58 - \frac{22}{24} \times 3$ and "55.25"-45 = <u>10.25</u> (cm)	M1 A1 (4)					
(d)	$\frac{"55.25"-2("51")+45}{"55.25"-45}$ [= -0.17073 < 0] negative [skew].	M1 A1ft					
	Notes	(2)					
(a) (b)	 M1 allow equivalent eg 16.5×³/₂ A1 for 24.75 allow 24.8 M1 correct method for finding the frequency density or area for the highest and 2nd highest bars Allow if 8 and 7 seen or 33 and 48.125 seen or 9.625 rather than 48.125 and/or 11 seen rather than 33 						
(c)(i) (ii)	dM1 dep on previous M mark awarded. A fully correct expression for <i>h</i> or a fully correct equation to enable <i>h</i> to be found eg $\frac{"33"}{10 \times 3} = \frac{"48.125"}{5h}$ A1 8.75 oe NB answer of 8.75 seen as final answer 3/3 M1 for $50 + \frac{7}{35} \times k$ or $55 - \frac{28}{35} \times k$ or $\frac{Q_2 - 50}{k} = \frac{60 - 53}{88 - 53}$ or $\frac{55 - Q_2}{k} = \frac{88 - 60}{88 - 53}$ where $4 \le k \le 6$ oe (condone use of $n + 1$ ie 7.5 rather than 7, 27.5 rather than 28 or 60.5 rather than 60) A1 51 (condone for use of $n + 1$ awrt 51.1) M1 $55 + \frac{2}{24} \times t$ or $58 - \frac{22}{24} \times t$ or $\frac{Q_3 - 55}{t} = \frac{90 - 88}{112 - 88}$ or $\frac{58 - Q_3}{t} = \frac{112 - 90}{112 - 88}$ oe where $2 \le t \le 4$ and using "their Q_3 "-45						
	(condone use of $n + 1$ ie 2.5 or 2.75 rather than 2, 21.5 or 21.25 rather than 22 or 9 90.75 rather than 90) A1 10.25 oe eg 41/4 allow 10.3 from correct working	0.5 or					

(d)	M1 substitution of their values from (c) seen or awrt -0.17 or $-7/41$
	A1ft dependent on M1 being scored. Correct description of skewness consistent with their values
	from part (c) ignore the final answer if working shown. Only allow no skew or symmetrical if
	their value should be 0 Ignore correlation.

Question Number	Scheme	Marks				
2. (a)	$[S_{tt} =]82873 - \frac{1361^2}{42}$ $[S_{ct} =]83634 - \frac{1634 \times 1361}{42}$	M1				
	$\begin{bmatrix} S_{tt} = \end{bmatrix} 82873 - \frac{1361^2}{40} \qquad \begin{bmatrix} S_{ct} = \end{bmatrix} 83634 - \frac{1634 \times 1361}{40} \\ \begin{bmatrix} S_{tt} = \end{bmatrix} 36564.975 \qquad \begin{bmatrix} S_{ct} = \end{bmatrix} 28037.15 \end{bmatrix}$	A1 A1 (3)				
(b)	$[r =] \frac{'28037.15'}{\sqrt{28732.1 \times '36564.975'}} = 0.865$ awrt <u>0.865</u>	M1 A1				
(c)	In general, films with higher cost have higher ticket sales .	(2) B1ft (1)				
(d)	$[b=]\frac{'28037.15'}{28732.1}[=0.9758]$	M1				
	$[a=]\frac{1361}{40}-b'\times\frac{1634}{40}$ or $34.025-b''\times40.85$	M1				
	t = -5.8369 + 0.9758c * $t = awrt - 5.84 + awrt 0.976c*$	A1cso* (3)				
(e)	$t = -5.84 + 0.976 \times 90$ $t = \pounds 82 \text{ million}$ awrt $\pounds 82 \text{ million}$	M1 A1 (2)				
(f)	$\begin{array}{l} -5.84 + 0.976c < 0.8c \rightarrow 0.176c < 5.84 \\ c < 33.1818 \end{array} \qquad $	M1 A1 (2)				
	Notes	Total 13				
(a)	Mark part (a) and (b) together					
(b)	M1 valid attempt at <i>r</i> with their $S_{cc} \neq 28732.1$ and their $S_{ct} \neq 83634$ A1 awrt 0.865					
(c)						
(d)	M1 correct numerical expression for b ft their $S_{ct} \neq 83634$ Implied by awrt 0.97	58 or better				
	M1 attempt at <i>a</i> with their value of <i>b</i> substituted. Implied by awrt 5.837 or better A1*cso answer given so both method marks must be awarded and no incorrect working seen. Either $b = 0.9758$ (or better) or $a = 5.837$ (or better) must be seen somewhere along with the correct equation in <i>t</i> and <i>c</i> (do not allow fractions).					
(e)	M1 for substituting $c = 90$ into $t = awrt -5.84 + awrt 0.976c$ Implied by awrt 82 A1 £82 million (must include units. Allow 82 million pounds). Allow awrt £82 million					
(f)	M1 forming inequality (allow > or < or = or \leq or \geq) with 0.8 <i>c</i> A1 correct inequality in <i>c</i> (allow any letter) with awrt 33.2 (units not required). Do not allow as a fraction. Ignore any lower limit. Condone awrt 33200000 or awrt 33.2 million					

Question Number	Scheme	Marks				
3. (a)	$[\overline{x} =]\frac{-1.2}{8} [= -0.15]$ $\sum b = 21 \times 8 + 2 \times (-1.2) [= 10]$	65.6] M1				
	$\begin{bmatrix} \overline{x} = \end{bmatrix} \frac{-1.2}{8} \begin{bmatrix} = -0.15 \end{bmatrix} \qquad \qquad \sum b = 21 \times 8 + 2 \times (-1.2) \begin{bmatrix} = 16 \\ -0.15 \end{bmatrix} = \frac{\overline{b} - 21}{2} \text{ oe} \qquad \qquad \qquad \begin{bmatrix} \overline{b} = \end{bmatrix} \frac{165.6}{8}$	M1				
	= 20.7 (cm) A1				
	$\sqrt{1-1-(1-1)^2}$	(3)				
(b)	$\sigma_{x} = \sqrt{\frac{5.1}{8} - \left(\frac{-1.2}{8}\right)^{2}} \left[= \sqrt{0.615} = 0.784 \right]$ $\sigma_{b} = 2 \times 0.784'$	M1				
		M1				
	= awrt <u>1.57</u>	$\begin{array}{c c} (cm) & A1 \\ & (3) \end{array}$				
(c)(i)	$x_9 = 1.2 \rightarrow b_9 = 1.2 \times 2 + 21$ or $9 \times 21 - 8 \times 20.7$ [= 354.6]	M1				
	= <u>23.4</u> (0	cm) A1 (2)				
(ii)	$\sum x^2 = 5.1 + 1.2^2 \left[= 6.54 \right] \qquad \left[\Rightarrow \sigma_x = \sqrt{\frac{5.1 + 1.2^2}{9} - 0^2} \right]$	M1				
	$= \operatorname{awrt} 0.8$					
	Notes	(2) Total 10				
(a)	1^{st} M1 for correct expression for \overline{x} ignore 1^{st} M1 for correct explicitletter 1^{st} M1 for correct explicit	pression for $\sum b$				
	2 nd M1 Using equation. " \overline{x} " = $\frac{\overline{b} - 21}{2}$ where 2 nd M1 use of " $\sum b$ "	$ \div n$ where $ \sum b > 18$				
	$-1.2 < \overline{x} < 1.2$ Condone <i>b</i> rather than \overline{b} A1 20.7 oe					
(b)	1 st M1 correct method for σ_x or σ_x^2 or $5.1 = \frac{\sum b^2 - 42 \times "168.6" + 8 \times 4}{4}$	$\frac{41}{2}$ or $\sum b^2 = 3447.6$				
	2 nd M1 for use of 2 × their σ_x (or 4 × their σ_x^2) (adding 21 is M0) or					
	$\frac{"3447.6"}{8} - \left(\frac{"165.6"}{8}\right)^2 \text{ or } \sqrt{\frac{"3447.6"}{8} - \left(\frac{"165.6"}{8}\right)^2}$					
	A1 awrt 1.57 Allow $\frac{\sqrt{246}}{10}$ (allow s_b = awrt 1.68 or $\frac{4\sqrt{246}}{35}$ from an	n n - 1 method)				
(c)(i)	M1 for a correct equation using $x_9 = 1.2$ to enable b_9 to be found eg	$1.2 = \frac{b-21}{2}$				
	or a correct method to find $\sum x$ for the 9 squirrels. ft their 20.7 A1 23.4 oe					
(ii)	M1 for $5.1 + "(\pm 1.2)"^2 [= 6.54]$ seen ft their x_9 Condone $5.1 + (\pm 9.54)$	$6)^2 [= 97.26]$				
	A1 awrt 0.852 Allow $\frac{\sqrt{654}}{30}$ (allow $s_x = awrt 0.904$ from an $n - 1$ me	ethod)				

Question Number	Scheme	Marks						
4.	$[F(6) =] \frac{45}{77}$ and $[F(7) =] \frac{60}{77}$							
	$\begin{bmatrix} P(W=7) = F(7) - F(6) = \end{bmatrix} "\frac{60}{77} " - "\frac{45}{77} " \begin{bmatrix} =\frac{15}{77} \end{bmatrix} and$ $\begin{bmatrix} P(W=8) = F(8) - F(7) = \end{bmatrix} 1 - "\frac{60}{77} " \begin{bmatrix} =\frac{17}{77} \end{bmatrix}$	M1						
	$E(W) = 6 \times "\frac{45}{77}" + 7 \times "\frac{15}{77}" + 8 \times "\frac{17}{77}"$ [= 6 \times 0.5844 + 7 \times 0.1948 + 8 \times 0.22077]							
	$= \frac{73}{11} \text{ or awrt } \underline{6.64}$	A1						
	Notes	[4]						
	1 st M1 for $\frac{45}{77}$ and $\frac{60}{77}$ seen Allow awrt 0.58 and awrt 0.78. may be seen unsimplified Implied by 2 nd M1 or by seeing $\frac{15}{77}$ 2 nd M1 for " $\frac{60}{77}$ "-" $\frac{45}{77}$ " and 1-" $\frac{60}{77}$ " allow awrt 0.195 or 0.20 and awrt 0.22 ft their F(6) and F(7) if working shown 3 rd M1 for an attempt to calculate E(W) with P(W = 6) correct and the correct method or value for at least one of P(W = 7) or P(W = 8) A1 $\frac{73}{11}$ oe or awrt 6.64							

Question Number	Scheme	Marks				
5. (a)	$P(W > 70) = P\left(Z > \frac{70 - 80}{8} [= -1.25]\right)$	M1				
	= $P(Z > -1.25)$ or $P(Z < 1.25)$ = 0.8944 awrt <u>0.894</u>	A1 A1 (3)				
(b)		B1				
	$\pm \left(\frac{k-80}{8}\right) = \underline{1.0364}$	M1 B1				
	k = 88.29 awrt <u>88.3</u>	A1 (4)				
(c)	$P(W < 66) = P\left(Z < \frac{66 - 80}{8} [= -1.75]\right) [= 0.0401 \text{ (calc } 0.040059)]$	M1				
	$0.25 \times P(Z < -1.75) [= 0.010025 (calc 0.0100147)] $ or $0.25 \times (1 - P(Z < 1.75))$	dM1				
	$\frac{y-80}{8} = -2.32(63)$	M1 A1				
	y = 61.389 awrt <u>61.4</u>	A1 (5)				
	Notes	Total 12				
(a) (b)	M1 for standardising with 70, 80 and 8 (allow \pm) 1 st A1 $z = \pm 1.25$ 2 nd A1 awrt 0.894 (calc 0.894350) NB do not ISW so an answer of 0.1056 is A0 1 st B1 for either correct probability statement. Allow \leq for $<$ and \geq for $>$ (may be implied by $z =$ awrt 1.04) M1 standardising with 80, 8 and equating to z , where $1 < z < 2$ 2 nd B1 $z = \pm 1.0364$ or better (calc 1.036432) A1 awrt 88.3 (calc 88.291459) NB awrt 88.3 implies 1 st B1 and M1 but not the 2 nd B1 they could get B1M1B0A1					
(c)	(Answer only 88.291 to 88.292 scored 4 out of 4)					

Question Number	Scheme				
6. (a)(i)	[P(A) =] 0.25	B1			
(ii)	$\begin{bmatrix} \mathbf{P}(A \mid B) = \end{bmatrix} \mathbf{\underline{1}}$	B1			
(iii)	$\begin{bmatrix} \mathbf{P}(A \mid C) = \end{bmatrix} \mathbf{\underline{0}}$	B1			
		(3)			
(b)	$\frac{q}{q+r} = \frac{3}{5}$ 0.13+ p+s = $\frac{7}{10}$ p+q+r+s+0.12+0.13 = 1				
	$0.13 + p + s = \frac{7}{10}$	M1			
	p + q + r + s + 0.12 + 0.13 = 1	M1			
	Solving simultaneously to get				
	$\frac{q}{0.3 - 0.12} = \frac{3}{5} \text{ or } 0.3 = 0.12 + 1.5r + r \text{ or } 0.3 = 0.12 + q + \frac{2}{3}q \text{ oe}$	dM1			
	$q = \underline{0.108}$ $r = \underline{0.072}$	A1 A1 (6)			
(c)	$\frac{5}{8} = 0.13 + 0.12 + 0.072 + s$ oe	M1			
	$s = \underline{0.303}$	A1 (2)			
	Notes	Total 11			
(a)(i) (ii) (iii)	B1 0.25 oe B1 1 cao B1 0 cao				
(iii) (b)	3				
	2^{nd} M1 correct expression for P(B' \cap D') = $\frac{7}{-1}$				
	$\begin{bmatrix} 2 & \text{MI} & \text{correct expression for } I(B + 1B) & 10 \\ 3^{\text{rd}} & \text{M1} & \text{A correct equation or use of sum of probabilities} = 1 \\ \text{must imply correct equation eg may ft their} \\ P(B' \cap D') &= \frac{7}{10} \text{ Implied by } q + r = 0.18 \end{bmatrix} \text{NB} \frac{3}{10} = 0.12 + q + r \text{ is} \\ 2ndM1 & 3rdM1 \end{bmatrix}$				
	or $P(D) = 0.18$ 4 th dM1 (dep on all 3 previous M1 being awarded) solving to obtain a correct equivisingle variable. Implied by a correct value for <i>q</i> or <i>r</i>	ation in a			
	$1^{\text{st}} \text{A1} q = 0.108 \text{ or } \frac{27}{250} \text{ oe}$				
	$2^{nd} A1 r = 0.072 \text{ or } \frac{9}{125} \text{ oe}$				
(c)	M1 correct expression for $P(B \cup C') = \frac{5}{8}$ ft their value for <i>r</i> . Allow use of the let	ter r			
	eg $\frac{5}{8} = 0.13 + 0.12 + r + s$ oe We will condone values of r outside the range 0	< <i>r</i> <1			
	A1 $s = 0.303$ oe				

Question Number	Scheme						Marks	
7. (a)	$\left[\frac{0.1}{0.8}\right] = \frac{1}{8}$					В	1 (1)	
(b)	$[0^2 \times 0.1 +]5^2 \times 0.2$	$2+10^2 \times 0.7 =$	75*				В	1*cso
(c)	$E(X) = [0 \times 0.1+] 5 \times 0.2 + 10 \times 0.7 [= 8]$ Var(X) = 75-('8') ² Var(X) = <u>11</u>				M M A	I1 1		
(d)	$Var(4-3X) = 3^{2} \times Var(X)[=3^{2} \times "11"]$ = <u>99</u>					M	(3) [1] [1ft (2)	
(e)	$ \begin{array}{l} P((0,5),(0,10),(5,10)) \\ = 0.1 \times 0.2 + 0.1 \times 0.7 + 0.2 \times 0.7 \\ [= 0.02 + 0.07 + 0.14] \\ = \underline{0.23} \end{array} \qquad \begin{array}{l} P((0,0),(5,5),(10,10) \\ = 1 - (0.1^2 + 0.2^2 + 0.7^2) \\ [= 0.5(1 - (0.01 + 0.04 + 0.49))] \\ = \underline{0.23} \end{array} $					M	11M1	
(f)	Products: 0, 25, 5 P(D = 0) = 0.1 + 0 $P(D = 50) = 2 \times 0$).1-0.1×0.1[2		B	(3) 1 11 M1
	$\begin{array}{c} D \\ P(D=d) \end{array}$	0 0.19	25 0.04	50 0.28		100 0.49		1 (4)
			Notes				Т	otal 14
(a)	B1 $\frac{1}{8}$ oe Allow	0.125 Do not	ISW					
(b)	B1*cso correct e	-					×0.7 =	75
(c)	M1 correct method to find mean. If no method seen award if 8 is seen M1 attempt at expression for variance ie 75 –(their $E(X)$) ² A1 11 cao							
(d)	M1 Use of $(-3)^2 \times \text{Var}(X)$ (condone 3 rather than -3 and missing bracket if final answer is correct) or $4^2 \times 0.1 + (-11)^2 \times 0.2 + (-26)^2 \times 0.7 - (-20)^2$ condone 11, 26 and 20 A1ft 99 or ft 9 × 'their (c)'							
(e)	1 st M1 for at least one correct product. NB may be combined eg 0.3×0.7 but not in the numerator or denominator of a fraction 2 nd M1 a fully correct expression oe e.g. $0.1 \times 0.2 + 0.3 \times 0.7$ A1 0.23 oe							
(f)	B1 all 4 correct products with no incorrect extras unless they have a probability of 0 associated with them 1^{st} M1 A correct method to find 1 of the 4 probabilities. Does not need to be associated with the correct product ALT P(D = 0) = $0.1 \times 0.1 + 2 \times 0.1 \times 0.2 + 2 \times 0.1 \times 0.7$ [= 0.19]							
	 2nd M1 A correct method to find 3 of the 4 probabilities or 2 of the 4 probabilities if the total of the 4 probabilities is 1 Must be associated with the correct product A1 all four correct probabilities (oe) associated with the correct products 							

Pearson Education Limited. Registered company number 872828 with its registered office at 80 Strand, London, WC2R 0RL, United Kingdom